

# 4 Deep Generative Models

BVM 2018 Tutorial: Advanced Deep Learning Methods

Jens Petersen

*Dept. of Neuroradiology, Heidelberg University Hospital*

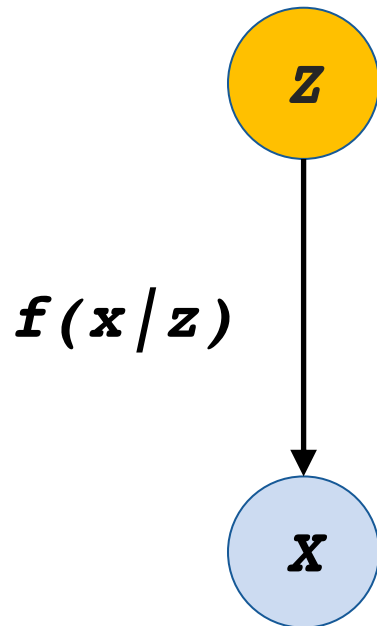
*Div. of Medical Image Computing, DKFZ Heidelberg*

*Faculty of Physics & Astronomy, Heidelberg University*

**Data Shortage**

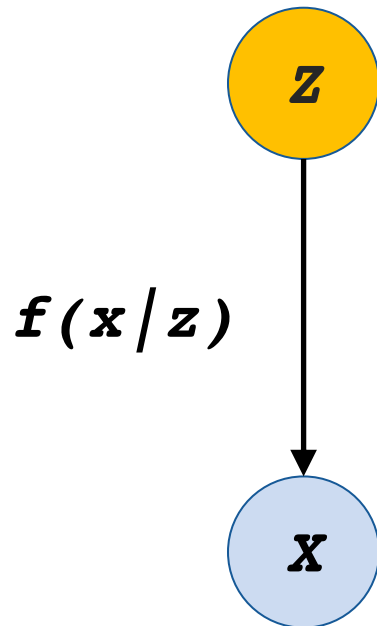
**Transfer learning**

**Noisy labels and data**



## Assumption

Observations  $x$  generated from latent variables  $z$  via mapping  $f$



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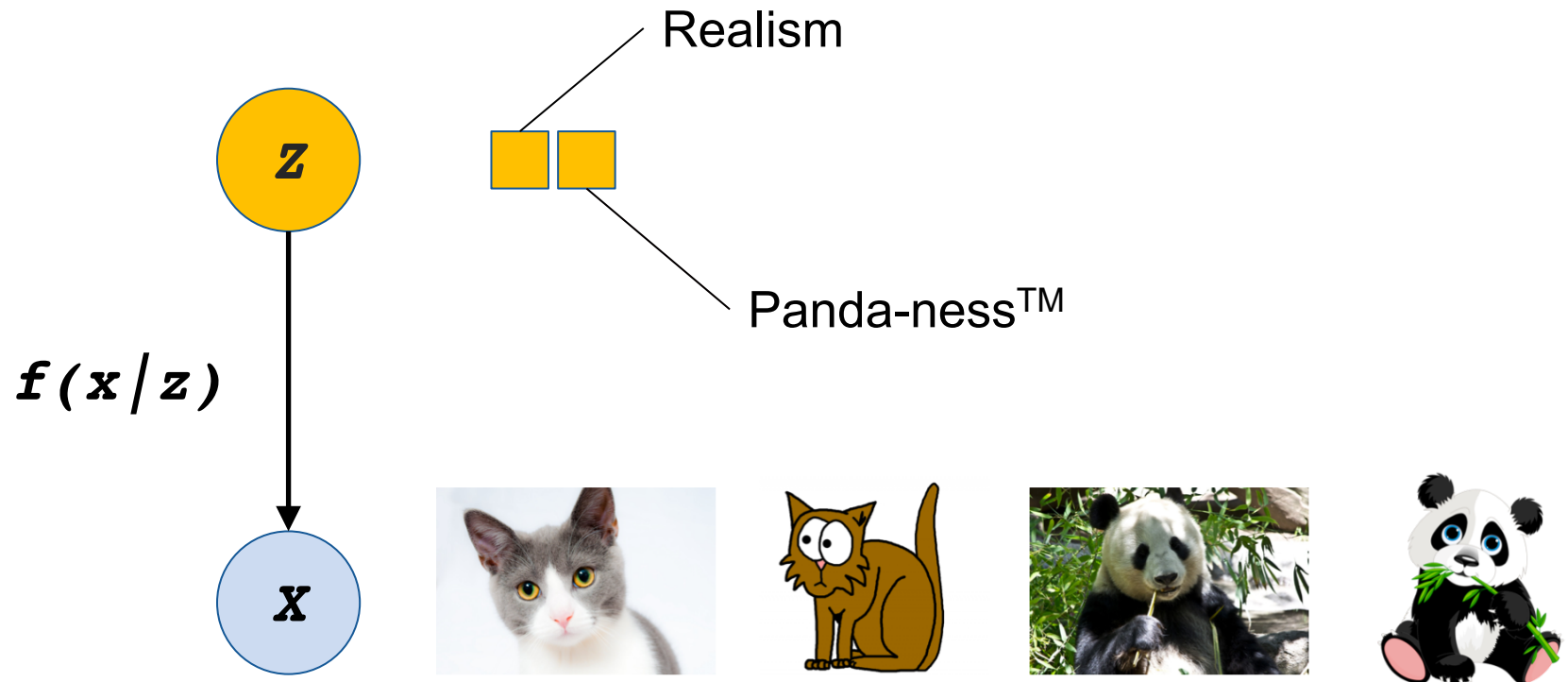
## Goal

- Be able to generate more samples that follow distribution of  $x$
- $z$  interpretable in some way





[pexels.com, pixabay.com, pngimg.com]



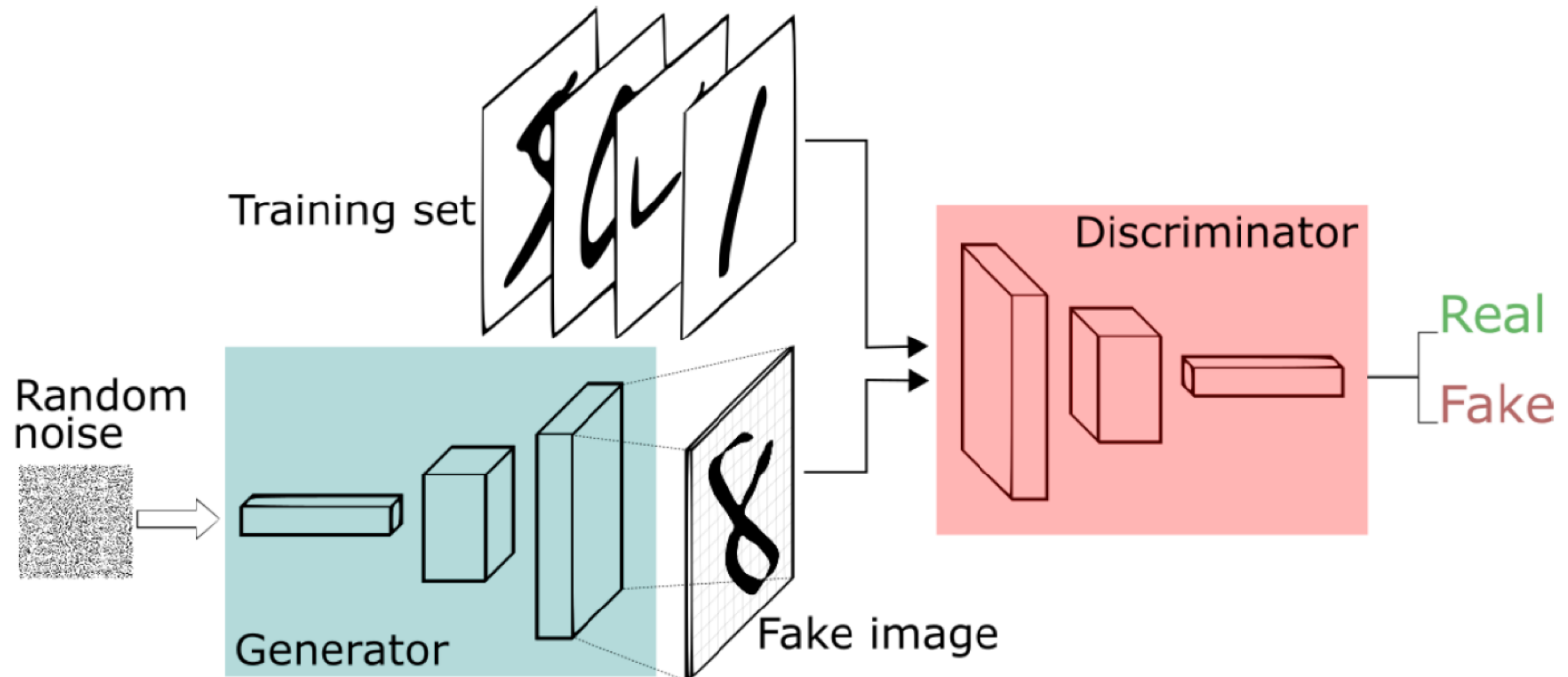
[pexels.com, pixabay.com, pngimg.com]

# Generative Adversarial Networks





[[https://twitter.com/goodfellow\\_ian](https://twitter.com/goodfellow_ian)]



[<https://deeplearning4j.org/generative-adversarial-network>]

[1] *Generative Adversarial Networks*, Goodfellow et al., 2014, NIPS

$$\min_G \max_D V(D, G) = \mathbb{E}_{\mathbf{x} \sim p_{\text{data}}(\mathbf{x})} [\log D(\mathbf{x})] + \mathbb{E}_{\mathbf{z} \sim p_{\mathbf{z}}(\mathbf{z})} [\log(1 - D(G(\mathbf{z})))]$$

D(real)  $\rightarrow$  1

D(fake)  $\rightarrow$  0

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D(fake)  $\rightarrow$  1

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Diagram illustrating the GAN learning objective with annotations:

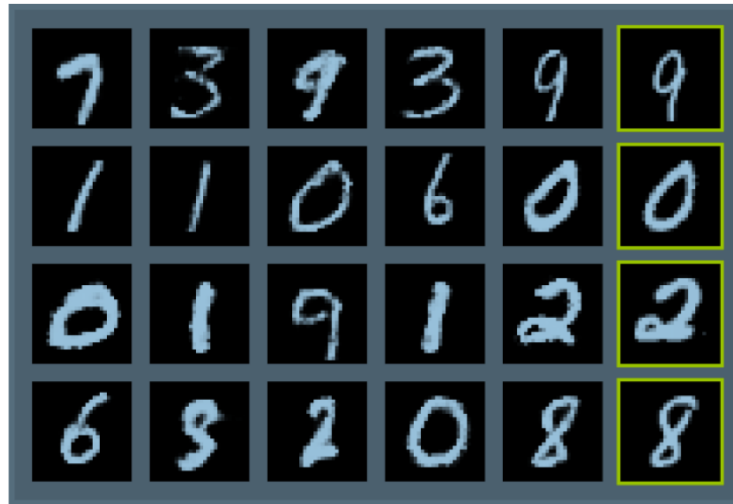
- $D(\text{real}) \rightarrow 1$  (Red text, pointing to  $\log D(\mathbf{x})$ )
- $D(\text{fake}) \rightarrow 0$  (Red text, pointing to  $\log(1 - D(G(\mathbf{z})))$ )
- $D(\text{fake}) \rightarrow 1$  (Green text, pointing to  $D(G(\mathbf{z}))$ )

- Trying to find saddle point  
→ Very hard to optimize
- Lot of work on different objectives and „tricks“ for training

[2] *Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks*

Radford et al., 2015, arXiv:1511.06434

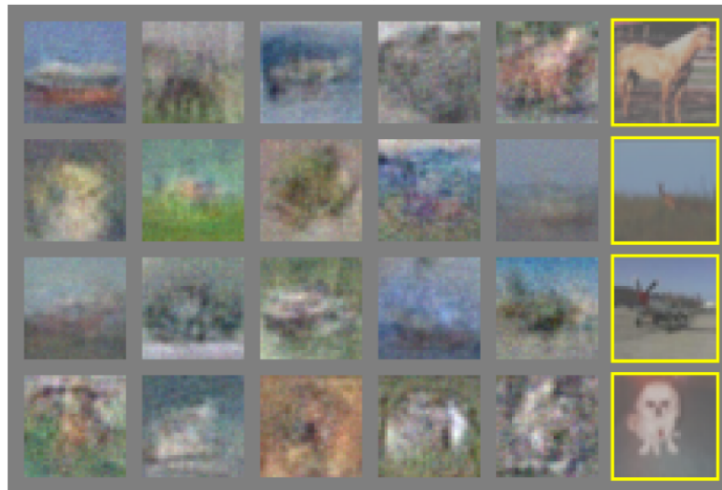
[3] *Are GANs Created Equal? A Large Scale Study*, Lucic et al., 2017, arXiv:1711.10337



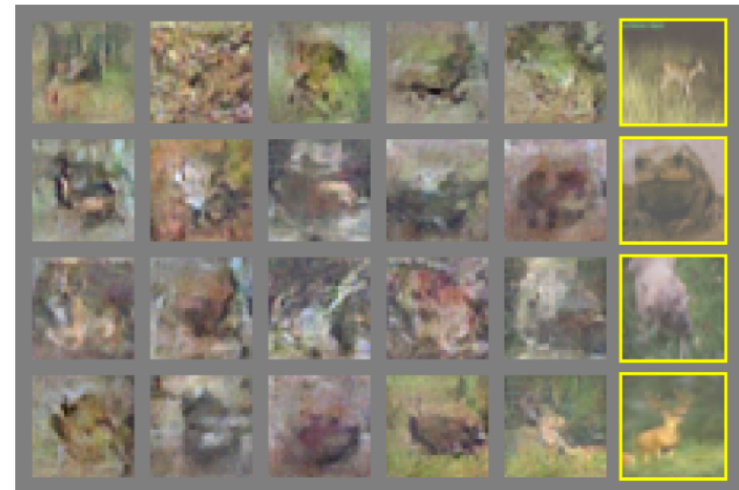
a)



b)



c)

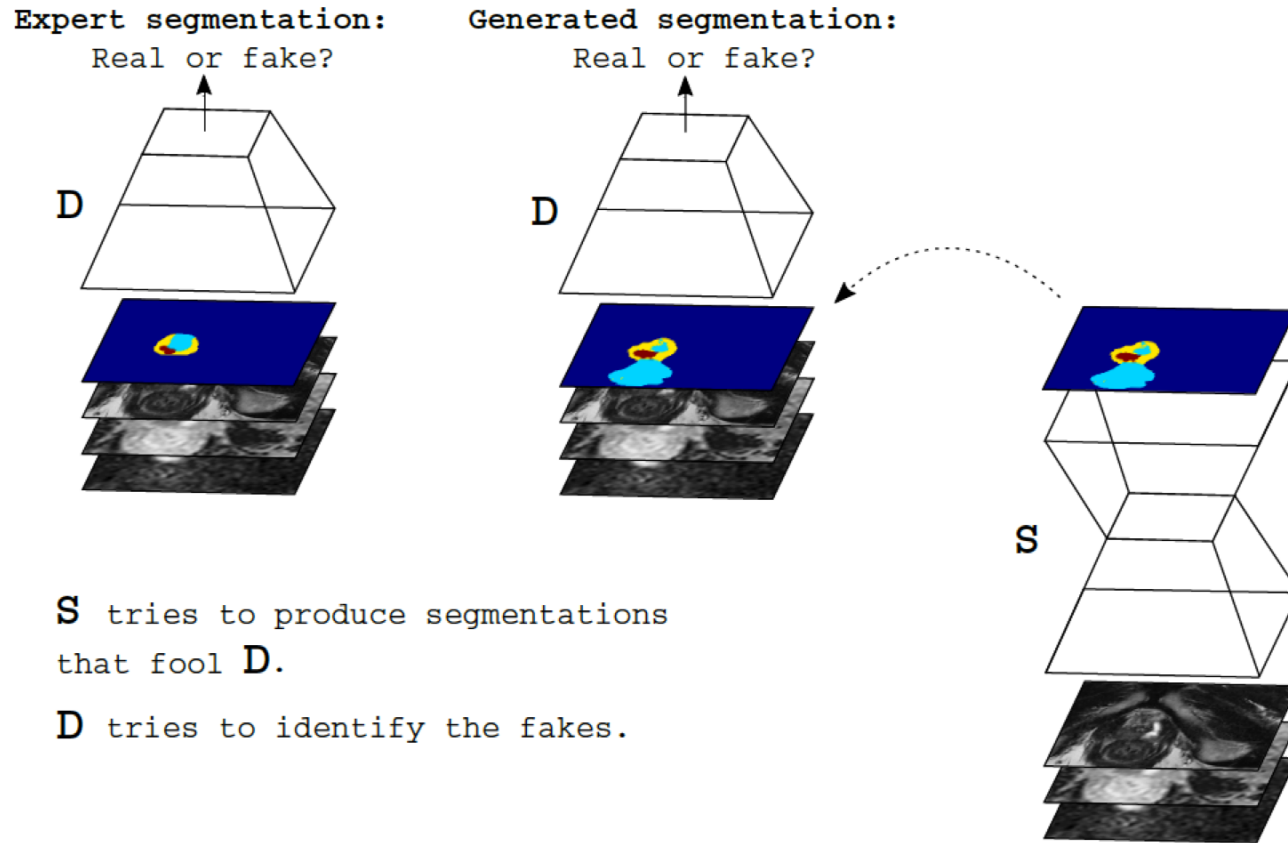


d)

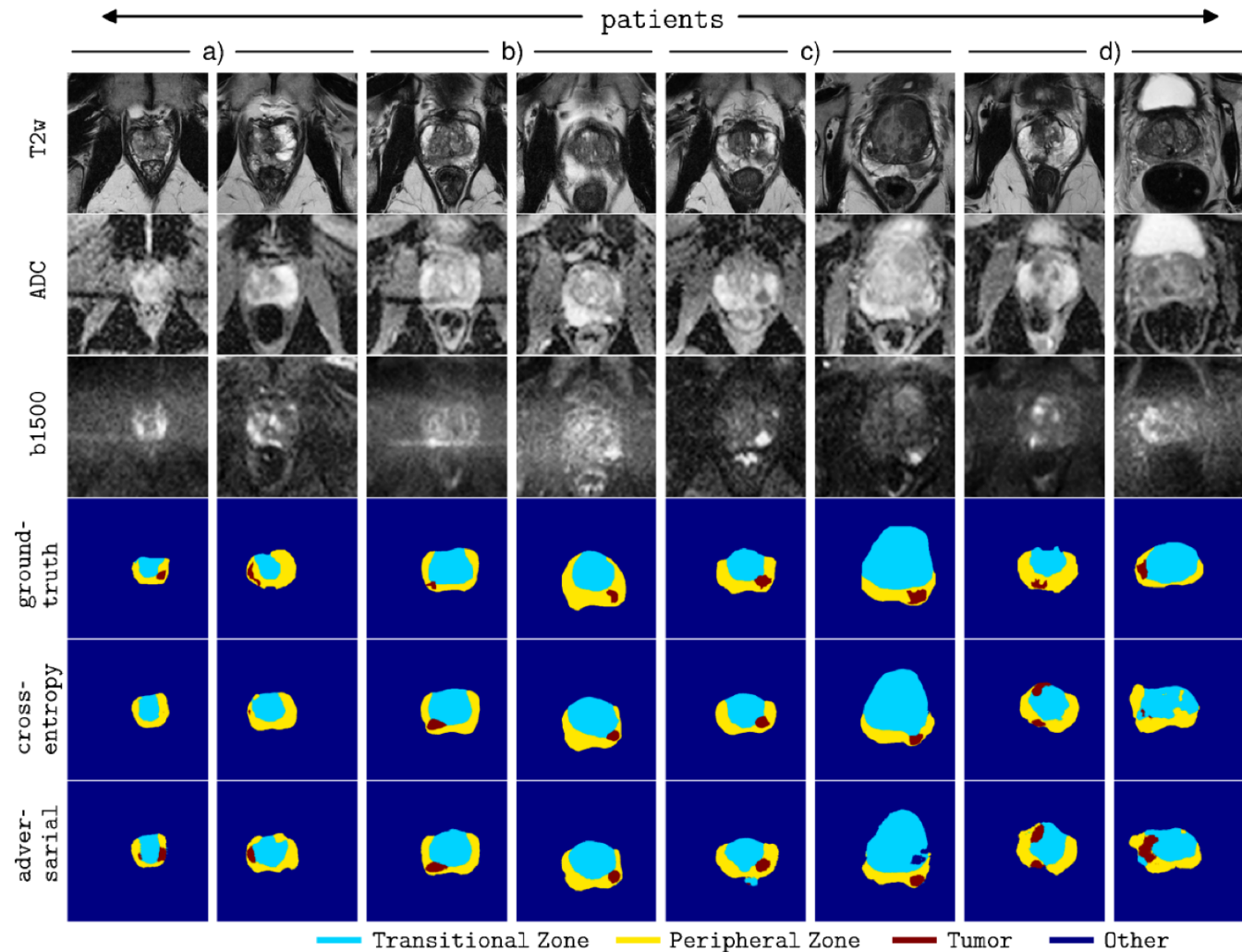
## **General case**

Generative models make no default assumptions for  $p(z)$

→ **Could be random noise and/or real data**



[4] *Adversarial Networks for the Detection of Aggressive Prostate Cancer*, Kohl et al., 2017, NIPS Workshop



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## **Assumption**

Have two unpaired sets A,B of images with some set-specific characteristic (e.g. photos & paintings)

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Be able to transform image so it looks like images in different set

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GANs that take images from A(B) and create images that similar to others from B(A)



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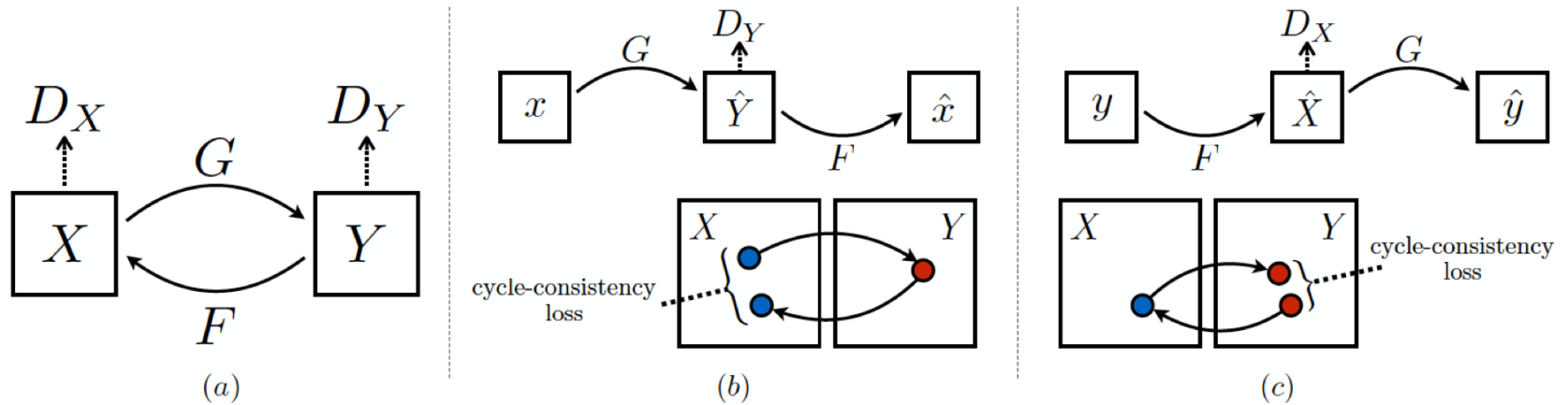
## **Goal**

Be able to transform image so it looks like images in different set

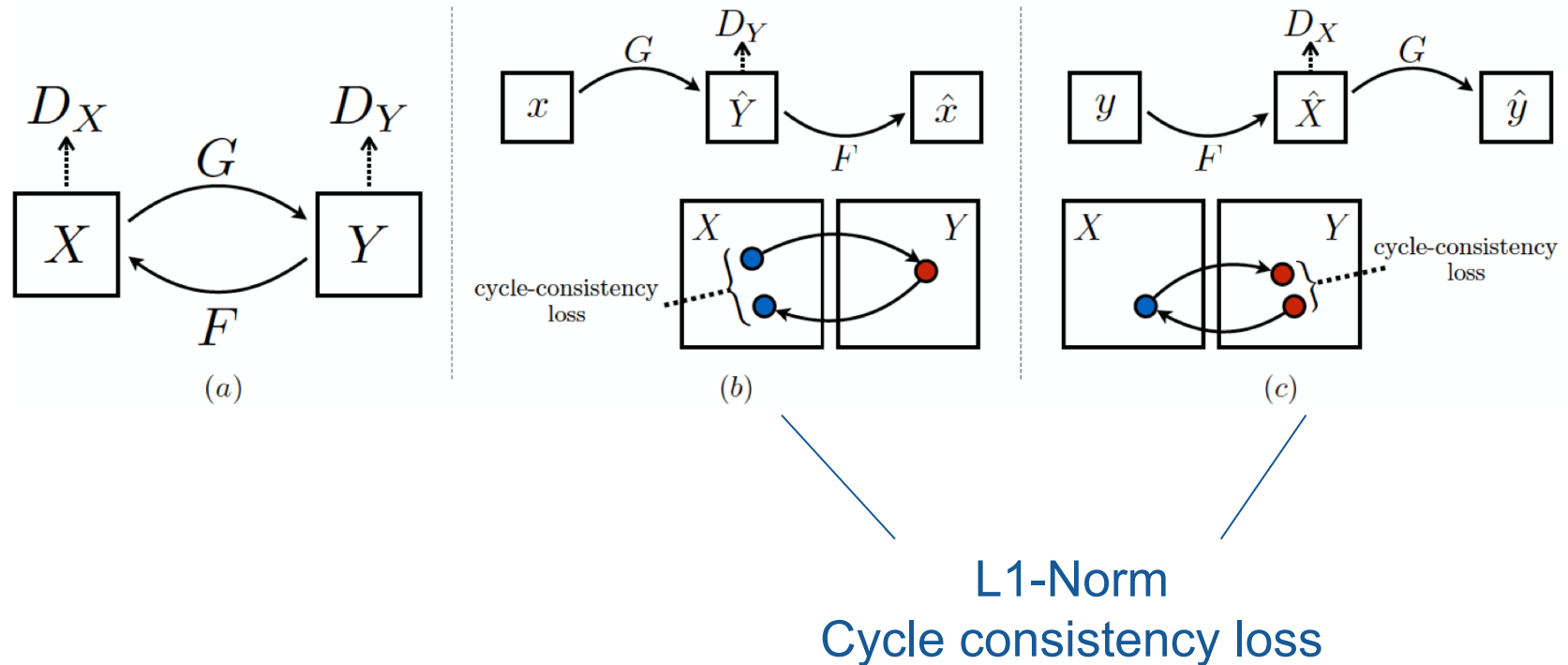
## **Naive Approach**

GANs that take images from A(B) and create images that similar to others from B(A)

→ **no guarantee that output looks similar to input**



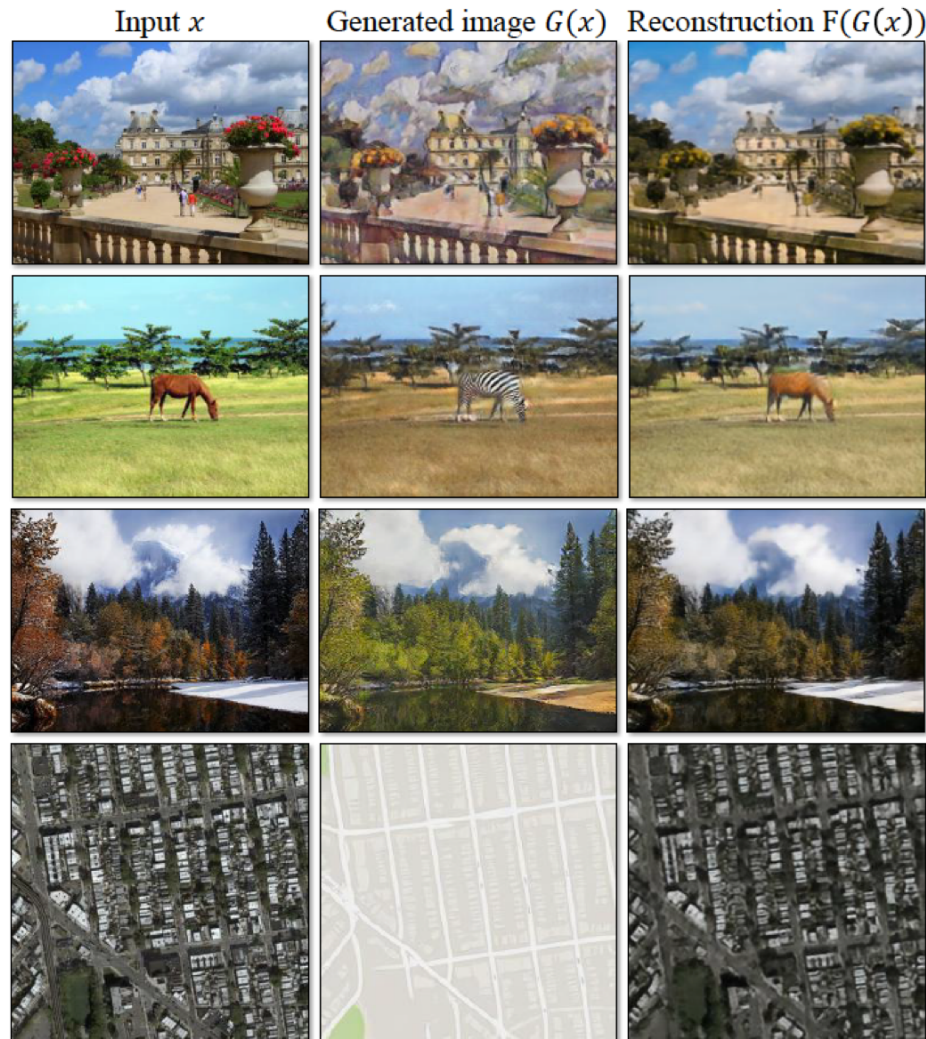
[5] *Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks*, Zhu et al., 2017, arXiv:1703.10593



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# Important Concepts CycleGAN

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[5] *Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks*, Zhu et al., 2017, arXiv:1703.10593



## PROGRESSIVE GROWING OF GANs FOR IMPROVED QUALITY, STABILITY, AND VARIATION

**Tero Karras**  
NVIDIA

**Timo Aila**  
NVIDIA

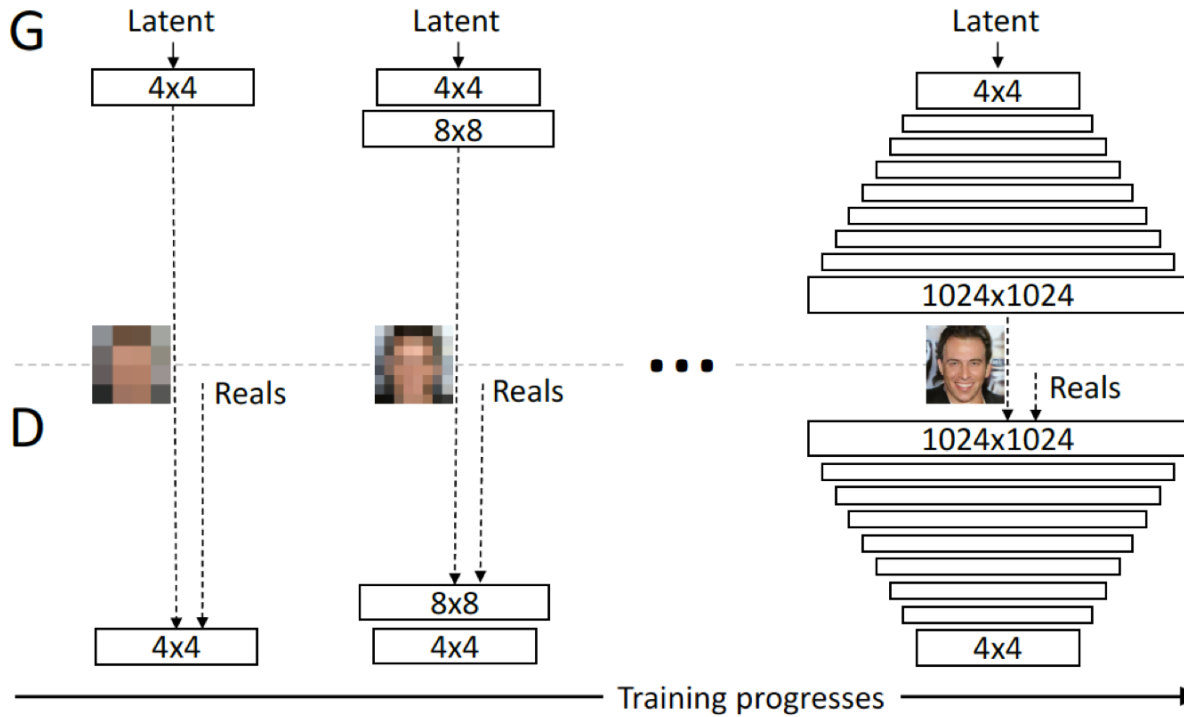
**Samuli Laine**  
NVIDIA

**Jaakko Lehtinen**  
NVIDIA and Aalto University

`{tkarras,taila,slaine,jlehtinen}@nvidia.com`

# Examples Progressive Growing

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Samples



Nearest Neighbours



- Pixel similarity
  - mean squared error (= L2 norm)
  - other norms

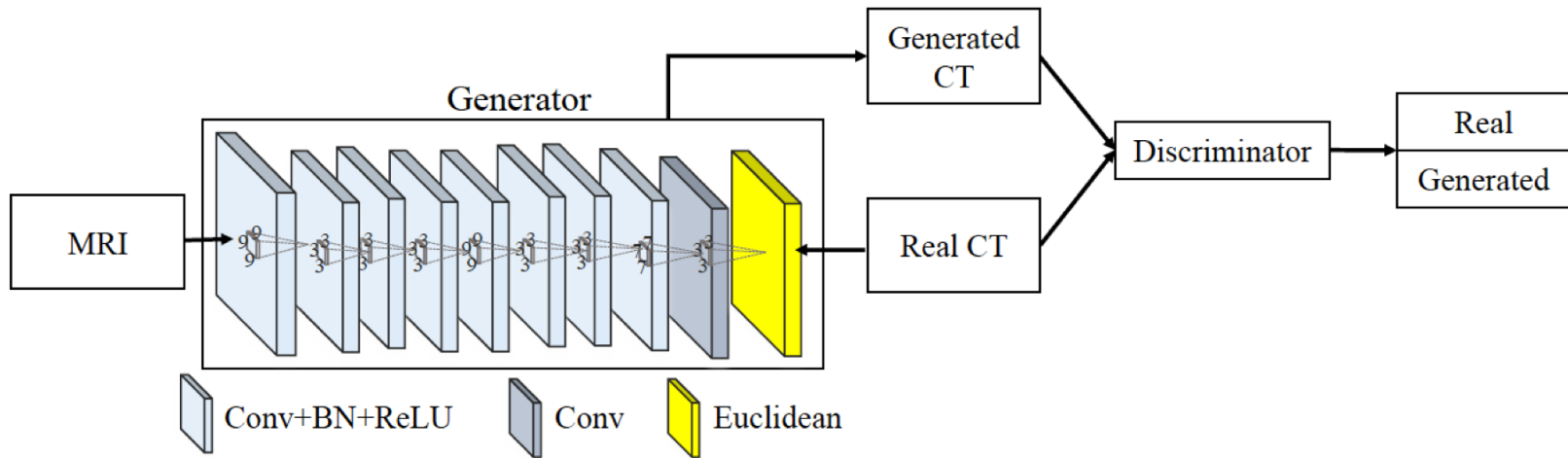
- Pixel similarity
  - mean squared error (= L2 norm)
  - other norms
- Semantic similarity
  - Inception score (score for entire model)
  - Combined distance of multiple feature layers in discriminator
  - Human evaluation (e.g. Mechanical Turk)

## Medical Image Synthesis with Context-Aware Generative Adversarial Networks

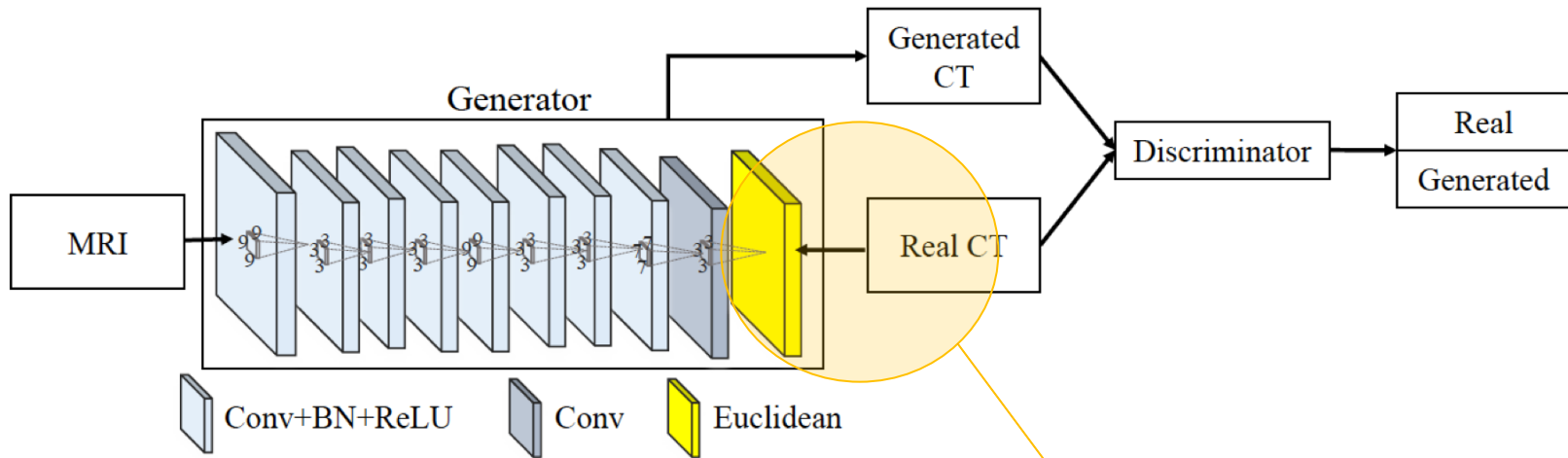
Dong Nie<sup>1\*</sup>, Roger Trullo<sup>2\*</sup>, Caroline Petitjean<sup>2</sup>, Su Ruan<sup>2</sup>, and Dinggang Shen<sup>1\*\*</sup>

<sup>1</sup> University of North Carolina at Chapel Hill, USA

<sup>2</sup> Normandie Univ, UNIROUEN, UNIHAVRE, INSA Rouen, LITIS, 76000 Rouen, France

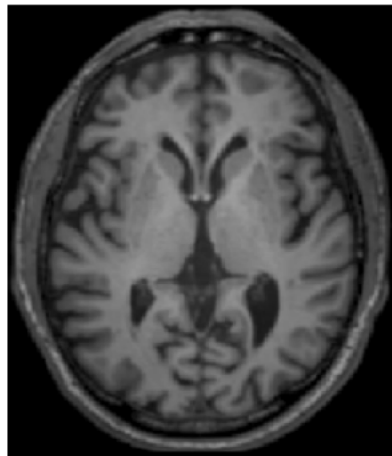


FCN architecture

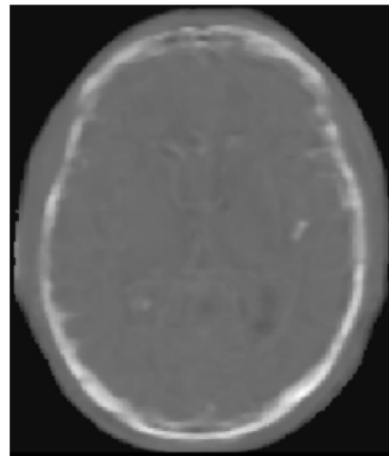


FCN architecture

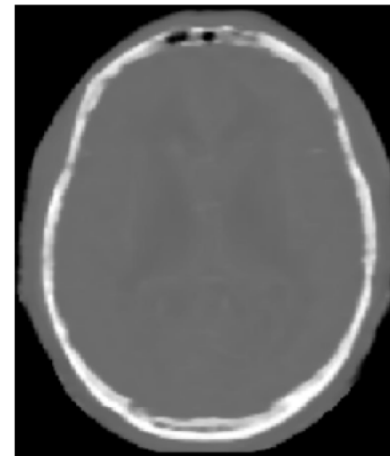
Combined adversarial & MSE loss



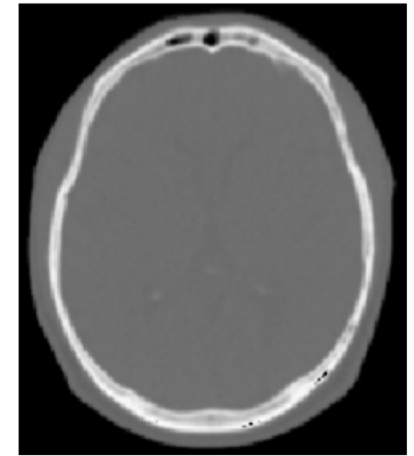
MRI



FCN



GAN



Ground Truth

## Unsupervised domain adaptation in brain lesion segmentation with adversarial networks

Konstantinos Kamnitsas<sup>1,4\*</sup>, Christian Baumgartner<sup>1</sup>, Christian Ledig<sup>1</sup>,  
Virginia Newcombe<sup>2,3</sup>, Joanna Simpson<sup>2</sup>, Andrew Kane<sup>2</sup>, David Menon<sup>2,3</sup>,  
Aditya Nori<sup>4</sup>, Antonio Criminisi<sup>4</sup>, Daniel Rueckert<sup>1</sup>, and Ben Glocker<sup>1</sup>

<sup>1</sup> Biomedical Image Analysis Group, Imperial College London, UK

<sup>2</sup> Division of Anaesthesia, Department of Medicine, Cambridge University, UK

<sup>3</sup> Wolfson Brain Imaging Centre, Cambridge University, UK

<sup>4</sup> Microsoft Research Cambridge, UK

## Assumption

$(X, Y)$  in source domain,  $(X^*)$  in target domain



## Assumption

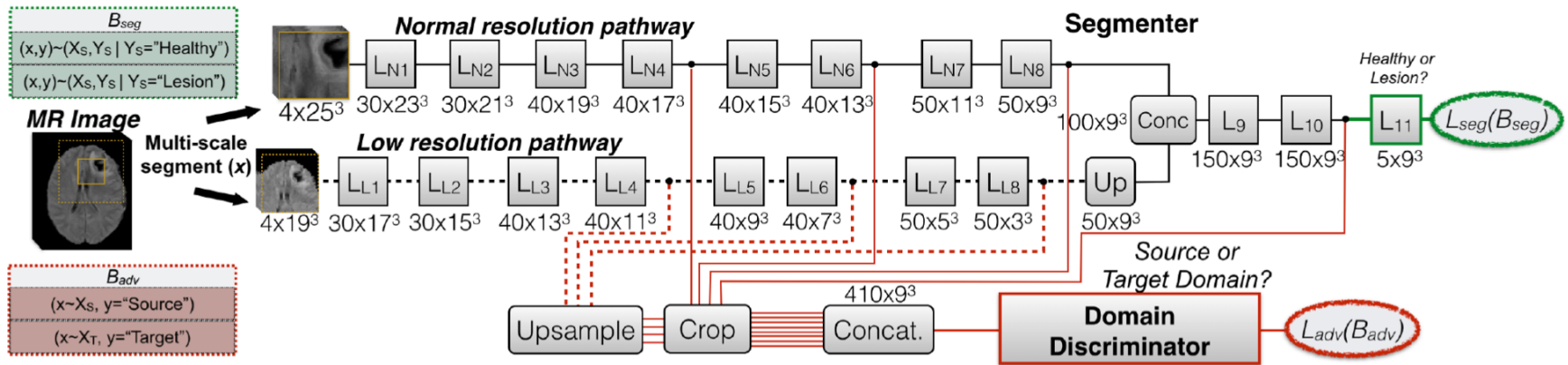
$(X, Y)$  in source domain,  $(X^*)$  in target domain

... + GE + Lesion Segmentation in source

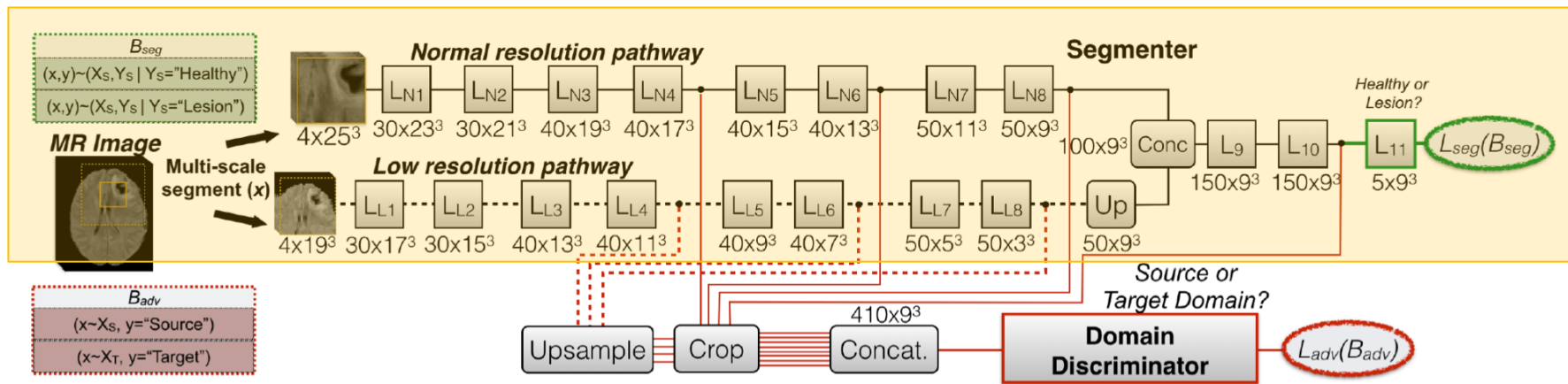
... + SWI in target

## Goal

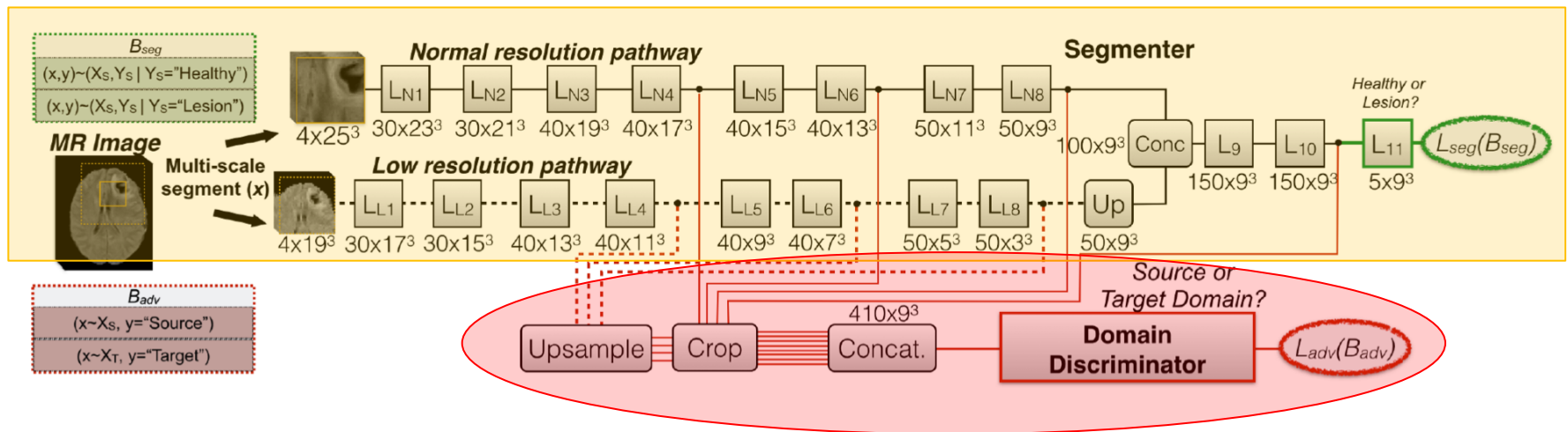
Segmentation in target domain



## DeepMedic architecture



## DeepMedic architecture



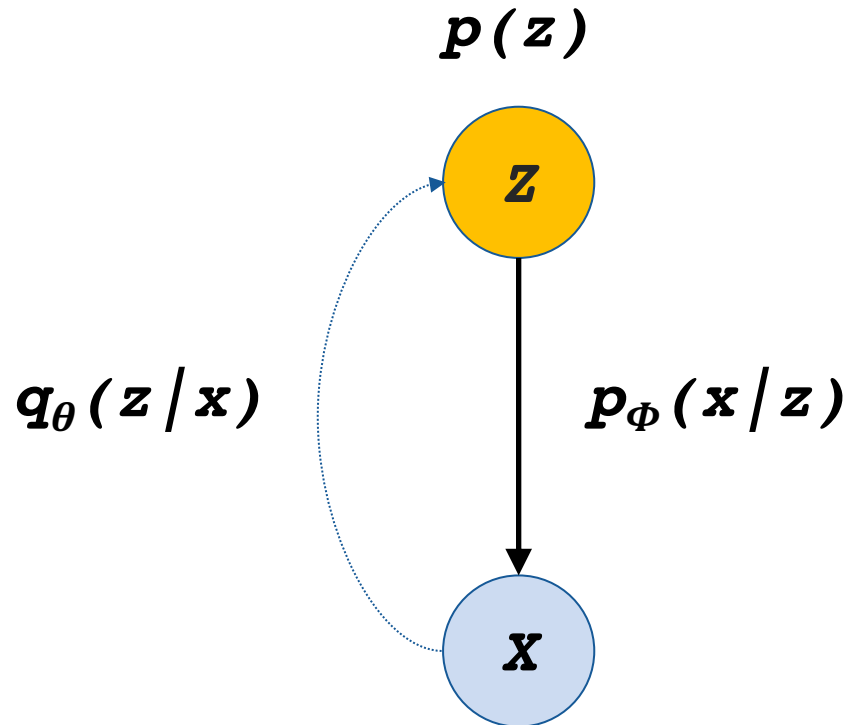
**Auxiliary adversarial loss  
ensures domain invariant feature maps**

	DSC
Train on S	15.7(13.5)
Train on S (No GE/SWI)	59.7(22.1)
<b>Train on S <math>\rightarrow</math> UDA to T (ours)</b>	<b>62.7(19.8)</b>
Train on T	63.5(20.2)
Train on S+T	66.5(17.7)
Train on S+T (GE/SWI diff chan.)	64.7(19.2)

Higher is better

- ✓ High-quality, high-resolution outputs possible
- ✓ Adversarial training extremely versatile
- ✗ Difficult to train
- ✗ No inference (latent representation from data)

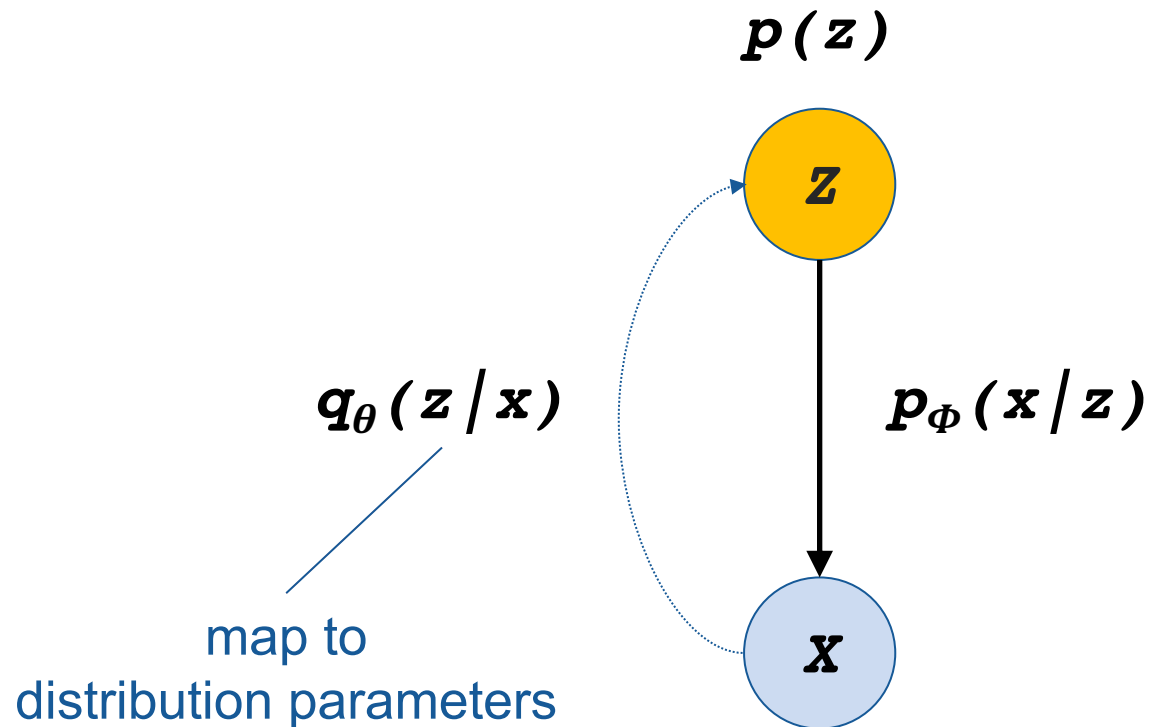
# Variational Autoencoders



[6] *Auto-encoding variational Bayes*, Kingma & Welling, 2014, ICLR

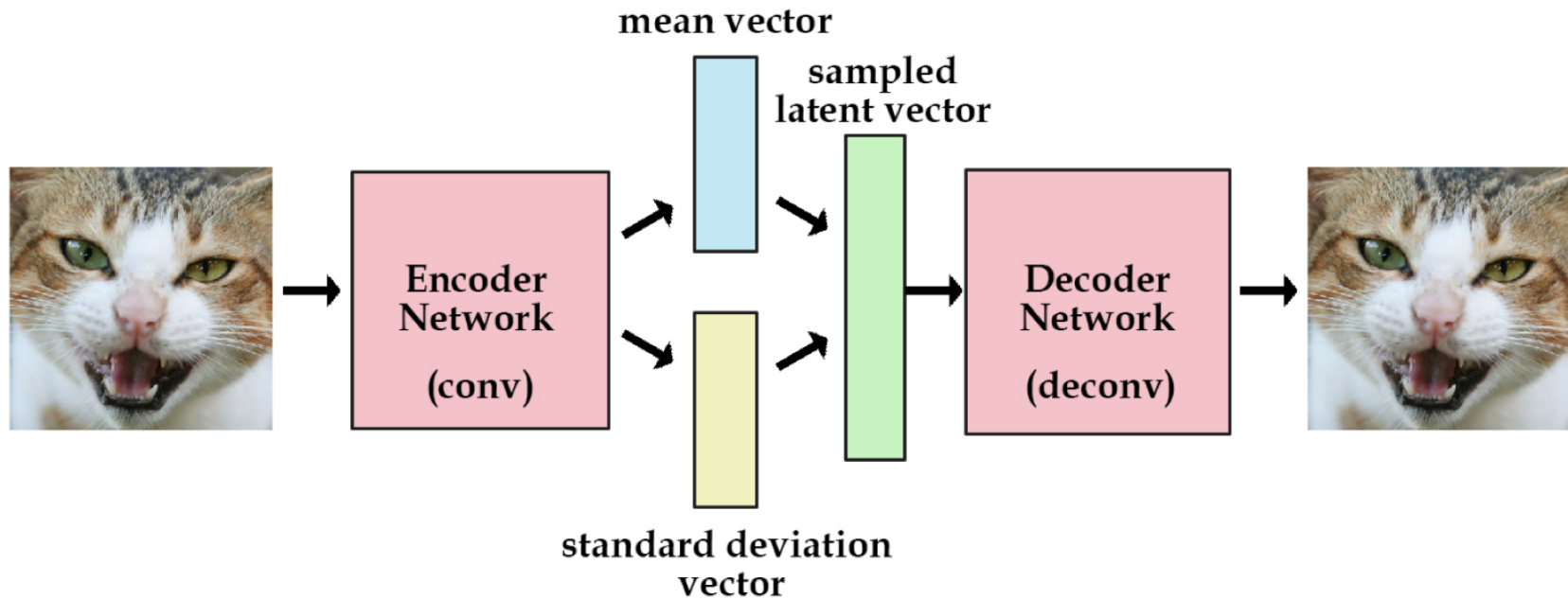
[7] *Stochastic backpropagation and approximate inference in deep generative models*, Rezende et al., 2014, ICML





[6] *Auto-encoding variational Bayes*, Kingma & Welling, 2014, ICLR

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[<http://kvfrans.com/variational-autoencoders-explained/>]

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$$z \sim \mathcal{N}(z; \mu, \sigma) \quad \longleftrightarrow \quad z = \mu + \sigma * \varepsilon \quad \varepsilon \sim \mathcal{N}(\varepsilon; 0, 1)$$

$$l_i(\theta, \phi) = -E_{z \sim q_\theta(z|x_i)}[\log p_\phi(x_i|z)] + KL(q_\theta(z|x_i) || p(z))$$

Maximize reconstruction fidelity (e.g. MSE)

$$l_i(\theta, \phi) = -E_{z \sim q_\theta(z|x_i)}[\log p_\phi(x_i|z)] + KL(q_\theta(z|x_i) || p(z))$$

Make encodings conform to prior





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## Learning Structured Output Representation using Deep Conditional Generative Models

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## Autoencoding beyond pixels using a learned similarity metric

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**Anders Boesen Lindbo Larsen<sup>1</sup>**

**Søren Kaae Sønderby<sup>2</sup>**

**Hugo Larochelle<sup>3</sup>**

**Ole Winther<sup>1,2</sup>**

ABLL@DTU.DK

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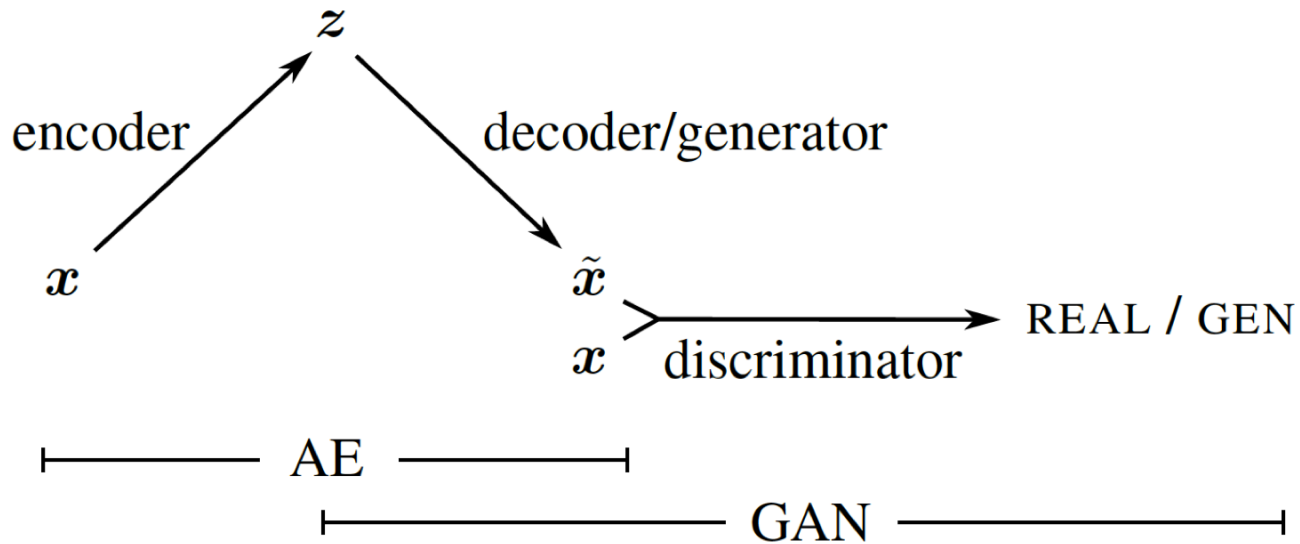
HLAROCHELLE@TWITTER.COM

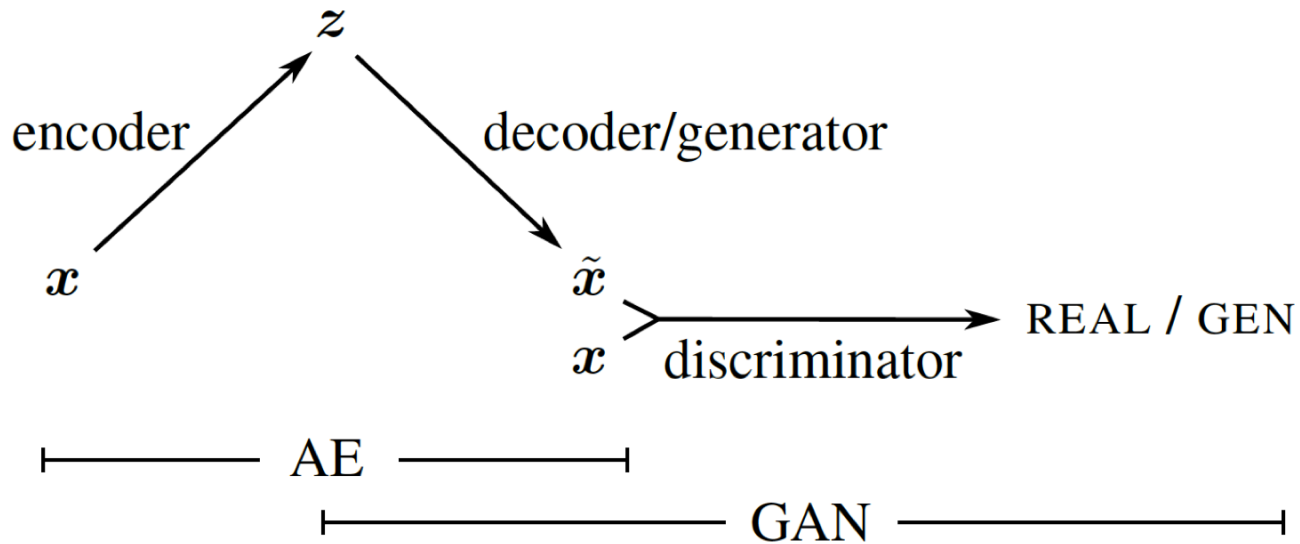
OLWI@DTU.DK

<sup>1</sup> Department for Applied Mathematics and Computer Science, Technical University of Denmark

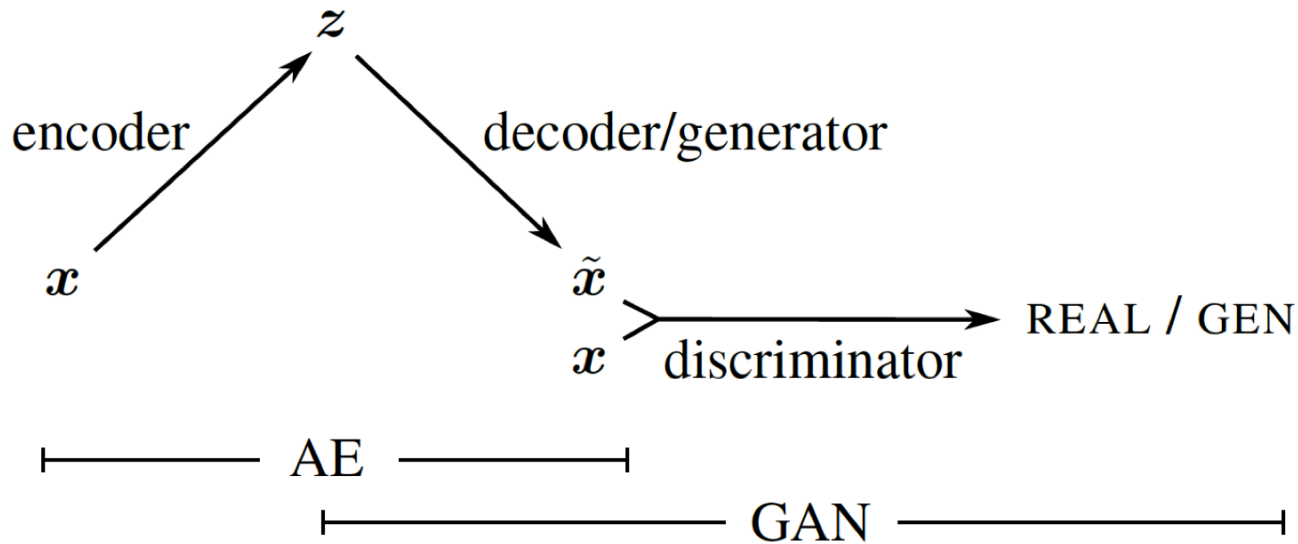
<sup>2</sup> Bioinformatics Centre, Department of Biology, University of Copenhagen, Denmark

<sup>3</sup> Twitter, Cambridge, MA, USA





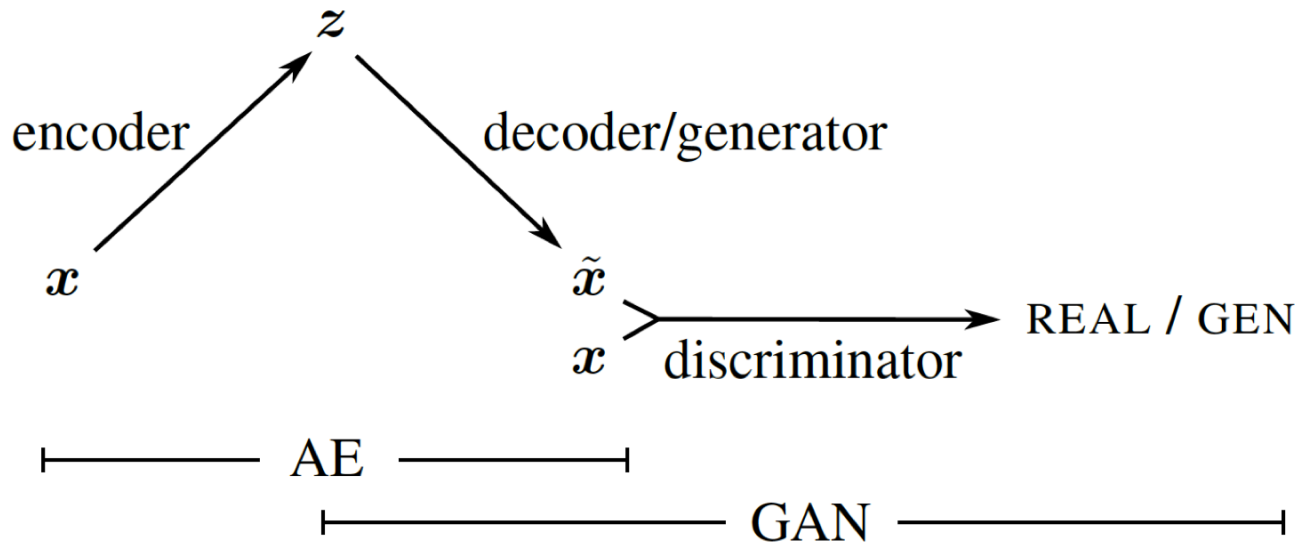
$$\mathcal{L}_{\text{VAE}} = \mathcal{L}_{\text{llike}}^{\text{pixel}} + \mathcal{L}_{\text{prior}}$$



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$$\mathcal{L}_{\text{llike}}^{\text{pixel}} = -\mathbb{E}_{q(z|x)} [\log p(x|z)] \longrightarrow \mathcal{L}_{\text{llike}}^{\text{Dis}_l} = -\mathbb{E}_{q(z|x)} [\log p(\text{Dis}_l(x)|z)]$$

$l$ -th layer discriminator



$$\mathcal{L}_{\text{VAE}} = \mathcal{L}_{\text{llike}}^{\text{pixel}} + \mathcal{L}_{\text{prior}}$$

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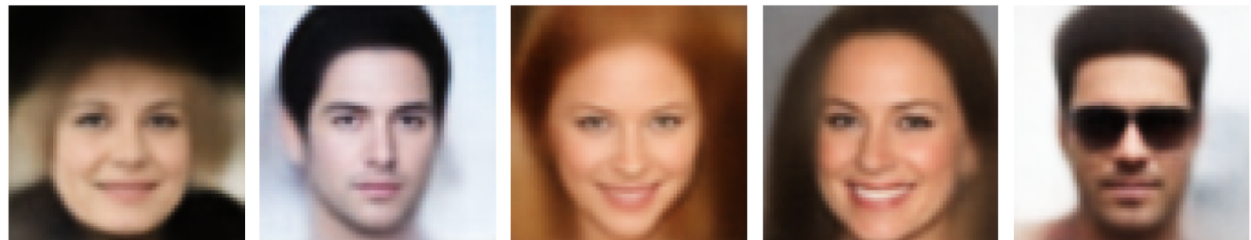
$$\mathcal{L} = \mathcal{L}_{\text{prior}} + \mathcal{L}_{\text{llike}}^{\text{Dis}_l} + \mathcal{L}_{\text{GAN}}$$

$l$ -th layer discriminator

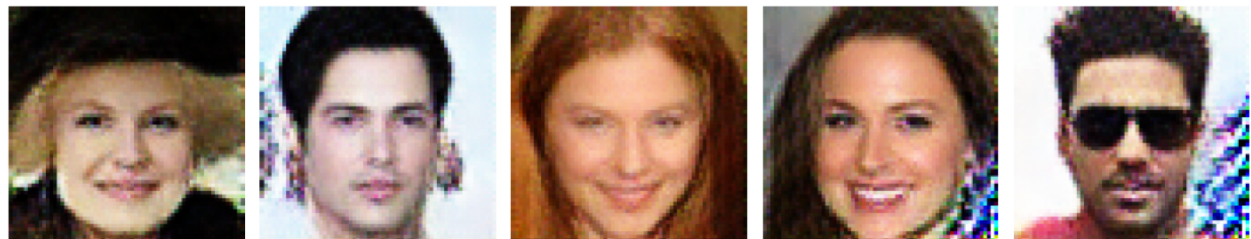
Input



VAE



$\text{VAE}_{\text{Dis}_l}$



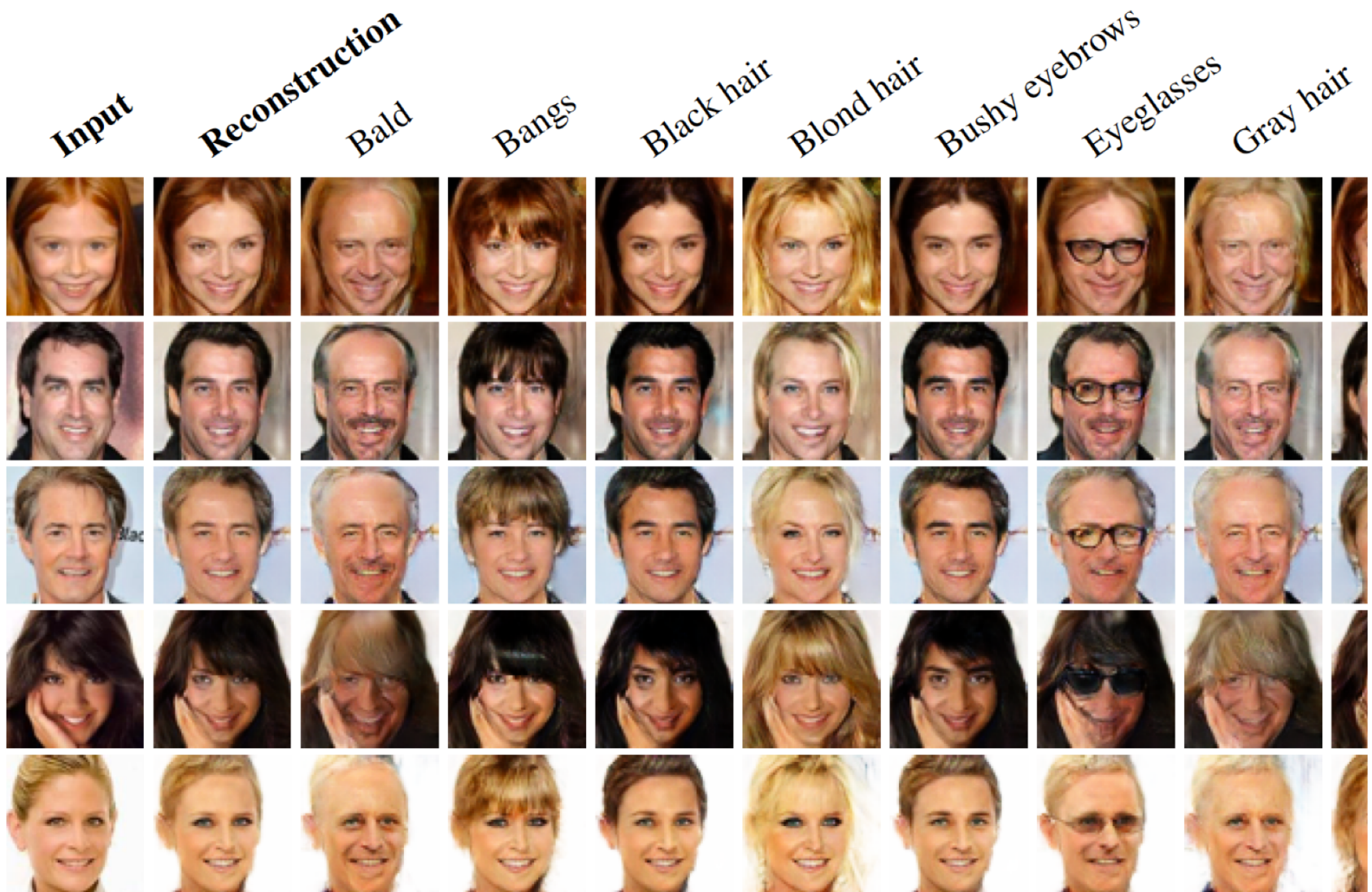
VAE/GAN





# Example Combining GANs & VAEs

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- GANs designed to generate new data
- VAEs designed to find interpretable latent representation

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  - can go from data to latent representation
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  - latent representation tends to focus on most important features

- GANs designed to generate new data
- VAEs designed to find interpretable latent representation
  - can go from data to latent representation
  - good for uncertainty estimation
  - latent representation tends to focus on most important features
- Hard to produce high quality outputs
  - Need better image similarity measure than MSE
  - Combination with GANs promising

- Literature overview GANs  
<https://github.com/nightrome/really-awesome-gan>
- Literature overview GANs for MIC  
<https://github.com/xinario/awesome-gan-for-medical-imaging>
- VAE Tutorial (Doersch)  
<https://arxiv.org/abs/1606.05908>
- PyTorch DCGAN  
<https://github.com/pytorch/examples/tree/master/dcgan>
- PyTorch VAE  
<https://github.com/pytorch/examples/tree/master/vae>
- Improving VAE outputs  
(Autoregressive flow) <https://arxiv.org/abs/1606.04934>  
(Normalizing flows) <https://arxiv.org/abs/1505.05770>
- Combining GANs and VAEs  
(Adversarial Autoencoder) <https://arxiv.org/abs/1511.05644>  
(Variational GAN) <https://arxiv.org/abs/1706.04987>
- Related generative models  
(NICE) <https://arxiv.org/abs/1410.8516>  
(Real NVP) <https://arxiv.org/abs/1605.08803>